## **Extreme vortex pinning in the noncentrosymmetric superconductor CePt<sub>3</sub>Si**

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We report on the vortex dynamics of a single crystal of the noncentrosymmetric heavy-fermion superconductor CePt<sub>3</sub>Si. Decays of the remnant magnetization display a logarithmic time dependence with rates that follow the temperature dependence expected from the Kim-Anderson theory. The creep rates are lower than observed in any other centrosymmetric superconductor and are not caused by high critical currents. On the contrary, the critical current in CePt<sub>3</sub>Si is considerably lower than in other superconductors with strong vortex pinning indicating that an alternative impediment on the flux-line motion might be at work in this superconductor.

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#### **I. INTRODUCTION**

Unconventional superconductors which violate spontaneously other symmetries beside the  $U(1)$ -gauge symmetry have been found to show many intriguing properties. Among such superconductors  $Sr<sub>2</sub>RuO<sub>4</sub>$ ,  $ProS<sub>4</sub>Sb<sub>12</sub>$ , and possibly  $UPt<sub>3</sub>$  have been identified as time-reversal symmetry breaking by means of zero-field  $\mu$ SR studies.<sup>1</sup> These compounds show surprisingly slow vortex dynamics with creep rates lower than in any other superconductor. $2-4$  $2-4$  It has been proposed that this behavior is connected with the presence of domain walls between different degenerate superconducting phases which would occur naturally in time-reversal symmetry-breaking states. Such domain walls could act as barriers for vortices, rather than the pinning of vortices at impurities and defects.<sup>5</sup> The latter pinning mechanism would have implied very high critical currents unlike what was observed in the experiments.

Our investigation of the heavy-fermion superconductor  $CePt<sub>3</sub>Si$  (Ref. [6](#page-3-5)) reveals extremely slow flux dynamics with creep rates even lower than those in  $Sr_2RuO_4$  $Sr_2RuO_4$  $Sr_2RuO_4$ ,<sup>2</sup>  $Pros_4Sb_{12}$ ,<sup>[3](#page-3-6)</sup> and  $UPt_3$ <sup>[4](#page-3-3)</sup>. Interestingly, the critical current in Ce $Pt_3Si$  is also low, in spite of the fact that this superconductor does not break time-reversal symmetry. Ce $Pt<sub>3</sub>Si$  is a member of a whole class of presumably unconventional heavy-fermion superconductors such as  $CeRhSi<sub>3</sub>$ ,<sup>[7](#page-3-7)</sup>  $CeIrSi<sub>3</sub>$ ,<sup>[8](#page-3-8)</sup> and UIr (Ref. [9](#page-3-9)) whose crystal lattices do not posses an inversion center. Among these noncentrosymmetric compounds,  $CePt<sub>3</sub>Si$  is the only one where superconductivity sets in already at ambient pressure. Unconventional features in the superconducting properties of systems without inversion symmetry has been discovered also outside the heavy-fermion class as, for example, in  $Li_2($ Pd,Pt $)_3B$  (Refs. [10](#page-3-10) and [11](#page-3-11)) or  $Mg_{10}Ir_{19}B_{16}$ .<sup>[12](#page-3-12)</sup>

In CePt<sub>3</sub>Si antiferromagnetic order sets in at a Néel temperature  $T_N$ = 2.2 K while the system adopts a superconducting ground state below a transition temperature  $T_c = 0.75$  K for polycrystalline samples.<sup>6</sup> Lower superconducting transition temperatures have been reported for single crystals.<sup>13</sup> Long-range magnetic order coexists with superconductivity on a microscopic scale as revealed by  $\mu$ SR investigations.<sup>14</sup> The upper critical field  $H_c \approx 3-5$  T exceeds the Pauli-Clogston limit  $H_P \approx 1.1$  T indicating that paramagnetic depairing is unimportant here. Knight-shift data actually display no reduction in the spin susceptibility below  $T_c$ , for magnetic fields perpendicular or parallel to the crystallographic *c* axis.[15](#page-4-2) Power laws describing the low-temperature behavior of thermal conductivity,  $\frac{16}{10}$  penetration depth,  $\frac{17}{1}$  1/*T*<sub>1</sub> relaxation rate,<sup>18</sup> and specific heat<sup>13</sup> observed in CePt<sub>3</sub>Si suggests a superconducting gap with line nodes. Remarkably,  $CePt<sub>3</sub>Si$  is the only heavy-fermion system to exhibit a Hebel-Slichter coherence peak below  $T_c$ ,<sup>[18](#page-4-5)</sup> a feature characteristic to an *s*-wave superconductor. The main part of this work is an experimental investigation of flux dynamics on a single crystal of  $CePt<sub>3</sub>Si$  which reveals the presence of an unconventional and very effective vortex-pinning mechanism.

## **II. CHARACTERIZATION OF THE SAMPLE AND THE SUPERCONDUCTING PHASE**

The high-quality CePt<sub>3</sub>Si single crystal investigated was grown using a Bridgman technique and the sample was ori-

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FIG. 1. (Color online) Temperature dependences of the real the imaginary part of the ac magnetic susceptibility across the superconducting phase transition. Inset: temperature dependence of the specific heat divided by temperature.

ented, cut, and polished in a parallelepiped shape with the dimensions 4.60 mm  $\times$  2.65 mm  $\times$  1.05 mm. The longer dimension is parallel to the crystallographic *a* axis while the smaller one is parallel to the *b* axis. An investigation of the single crystal for twinning (two distinct noncentrosymmetric atomic configurations) was performed by a new refinement of the crystal structure of CePt<sub>3</sub>Si from x-ray intensity data. It shows a contribution of 87% of the main inversion twin component.

Prior to the flux creep measurements the sample was characterized by ac magnetic susceptibility and specific heat. The investigation of vortex dynamics was performed in a dilution refrigerator in the temperature range  $0.1 \le T \le 0.5$  K with the sample enclosed in a custom-built mixing chamber and using a superconducting quantum interference device (SQUID) detector to determine the magnetic flux expelled. The external magnetic field applied to drive the sample into the Bean critical state was applied along the *a* axis. In the same experimental configuration, ac susceptibility experiments were performed in the temperature range  $0.025 \leq T$  $\leq$  2.4 K using an inductance bridge with a SQUID as null detector. A very low ac excitation field of *H*= 1.3 mOe was applied along the *a* axis at a frequency  $f = 80$  Hz. The temperature dependence of the specific heat was measured in the temperature range  $0.05 \le T \le 4.5$  K employing a quasiadiabatic pulse method.

Both, the real,  $\chi'$ , and the imaginary,  $\chi''$ , part of the ac susceptibility (Fig.  $1$ ) clearly reveal the superconducting transition with the midpoint of the anomaly in  $\chi'$  located at  $T_c$ = 0.45 K, a value much lower than the one obtained for polycrystals. The transition width, defined as the temperature difference between the 10% and 90% drop of the real part of susceptibility across the anomaly, is  $\Delta T = 0.1$  K also substantially smaller than the value observed for polycrystalline samples. Moreover, our finding is in excellent agreement with previous studies on high-quality single crystals.<sup>13</sup> The *T<sub>c</sub>* discrepancy between single crystal and polycrystal is not yet properly understood, but one possible explanation is that this compound has an homogeneity range<sup>19</sup> similar, for example, to the well-known case of  $CeCu<sub>2</sub>Si<sub>2</sub>,<sup>20</sup>$  $CeCu<sub>2</sub>Si<sub>2</sub>,<sup>20</sup>$  $CeCu<sub>2</sub>Si<sub>2</sub>,<sup>20</sup>$  which allows for homogeneous samples with slightly different compositions but substantially different physical properties to form. Another scenario<sup>21</sup> suggests that twin boundaries could enhance the trend to superconductivity in polycrystalline samples. Upon warming up the sample in the normal state,  $\chi'$  and  $\chi''$  become temperature independent up to *T*=2.4 K and no signature of the transition from the long-range magnetically ordered state into the paramagnetic phase was detected, for our field orientation  $(H \| a)$ .

The temperature dependence of the specific heat divided by temperature is depicted in the inset of Fig. [1.](#page-1-0) The transition into the antiferromagnetically ordered state is clearly visible as a sharp peak at  $T_N$ = 2.3 K, a value consistent with the one obtained in previous specific-heat studies.<sup>13</sup> Upon further cooling down, the system adopts a superconducting ground state at  $T_c = 0.42$  K, in good agreement with our sus-ceptibility data and Ref. [13.](#page-4-0) Both  $T_N$  and  $T_c$  are defined as the midpoint of the jump in *C* across the respective anomaly. The *C*/*T* data in the temperature range  $0.5 \le T \le 2.1$  K are well described by  $C/T = 423 \text{ mJ/(mol K}^2)$  $+140T<sup>2</sup>$  mJ/(mol K<sup>4</sup>). We remove the phononic and antiferromagnetic contributions to the specific heat by subtracting  $140T^3$  mJ/(mol K<sup>4</sup>) from the *C*(*T*) data and obtain a normalstate Sommerfeld coefficient  $\gamma_n = 400 \text{ mJ/(mol K}^2)$ . This leads to a jump of the specific heat at the superconducting phase transition of  $\Delta C / (\gamma_n T_c) \approx 0.29$ , a value situated significantly below the BCS-theory prediction of  $\Delta C/(\gamma_n T_c)$  $= 1.43$ . In the superconducting state, *C* exhibits a quadratic temperature dependence down to  $T=0.1$  K rather than an exponential one, indicative of the existence of line nodes in the superconducting gap. $22$  A zero-temperature interception of the quadratic specific heat would yield a residual electronic specific-heat coefficient with a finite value of  $\gamma_s$  $= 145$  mJ/mol K<sup>2</sup>. However, below  $T=0.1$  K, the specific heat has a weaker temperature dependence, therefore the residual  $\gamma_s$  will assume probably an even higher value and partially account for the very low value of  $\Delta C/(\gamma_n T_c)$ .

### **III. FLUX DYNAMICS MEASUREMENTS**

Isothermal relaxation curves of the remnant magnetization *M<sub>rem</sub>* were taken after cycling the specimen in an external dc magnetic field *H* applied along the crystallographic *a* direction. Vortices were introduced into the sample at a constant and slow rate in order to avoid eddy-current heating and using, at the lowest temperature, a magnetic field just high enough to drive the sample into the Bean critical state. The required magnetic field was kept constant in the sample for several minutes and then gradually reduced to zero. Immediately after, the relaxation of the metastable magnetization was recorded with a digital flux counter for several hours. The time required to ramp down the field is negligible compared with the time of the relaxation measurement. At the lowest temperature of our investigation, *T*= 100 mK, we determined the field corresponding to the Bean critical state,  $H^*$ , by estimating the field  $H_s$  where the remnant magnetization saturates as a function of the applied external magnetic field  $(H_s \approx 2H^*)$ . For this sample, we found  $H_s = 500$  Oe at  $T=100$  mK (inset of Fig. [2](#page-2-0)). At higher temperatures the sample is in the critical state already for smaller external

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FIG. 2. (Color online) Temperature dependence of the total remnant magnetization. Dashed line is a linear fit to the data. Inset: total remnant magnetization at *T*= 0.1 K and *T*= 0.2 K as function of the external magnetic field *H*.

fields since  $H<sub>s</sub>$  decreases upon increasing  $T$  as demonstrated in the inset of Fig. [2.](#page-2-0) In the main part of Fig. [2,](#page-2-0) we present the temperature dependence of the remnant magnetization obtained after cycling the sample in a field of *H*= 500 Oe. To obtain the value of  $M_{rem}$ , after removing the field at constant temperature we warmed up the sample well above  $T_c$  and recorded the total magnetic flux expelled.  $M_{rem}$  decreases monotonically upon increasing temperature with the experimental data well described by a linear fit dashed line in Fig. [2](#page-2-0)) which intercepts zero at around  $T \approx 0.41$  K. This is in excellent agreement with the value of  $T_c$  yielded by ac susceptibility and specific-heat measurements. In light of the comparison between the single-crystalline and polycrystalline CePt<sub>3</sub>Si samples, it is important to remark that at  $T$  $= 0.5$  K no flux was trapped in the crystal clearly showing that the bulk of the sample is well in the normal state at this temperature.

Isothermal decays of the remnant magnetization at different temperatures are depicted in Fig. [3.](#page-2-1) At constant temperature the flux escaping the sample is recorded typically for more than  $10^4$  s. Then the sample is heated up above  $T_c$  so all the trapped field is expelled out of the sample (inset of Fig. [3](#page-2-1)). In this way we obtain the value of the total remnant magnetization as the sum of the amount of flux expelled in the first  $10^4$  s plus the flux removed while crossing  $T_c$ . This value of  $M_{rem}$  is then used to normalize the creep rate. At all temperatures the decays show a logarithmic time dependence as predicted by the Kim-Anderson theory. $^{23}$  The creep rate becomes faster upon increasing the temperature as expected for thermally activated flux motion. The temperature dependence of the normalized relaxation rates  $S = \partial \ln(M) / \partial \ln(t)$ for CePt<sub>3</sub>Si is depicted in Fig. [4](#page-2-2) together with the rates obtained for the heavy-fermion superconductor  $UBe_{13}$  $UBe_{13}$  $UBe_{13}$  (Refs. 3) and [4](#page-3-3)) which only breaks gauge symmetry,  $Pros<sub>4</sub>Sb<sub>12</sub>$  (Ref. [3](#page-3-6)) which, in addition, violates time-reversal symmetry and the noncentrosymmetric superconductor  $Li<sub>2</sub>Pt<sub>3</sub>B<sup>.24</sup>$  $Li<sub>2</sub>Pt<sub>3</sub>B<sup>.24</sup>$  $Li<sub>2</sub>Pt<sub>3</sub>B<sup>.24</sup>$  Remarkably, CePt<sub>3</sub>Si has anomalously small decay rates comparable only with  $Li<sub>2</sub>Pt<sub>3</sub>B$  and lower by a factor of five than the very low creep rates observed in  $Pros_4Sb_{12}$ . Li<sub>2</sub>Pt<sub>3</sub>B breaks the

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FIG. 3. (Color online) Normalized remnant magnetization as a function of time at different constant temperatures. Inset: remnant magnetization as a function of time at *T*= 0.1 K. After 2.25  $\times 10^4$  s the sample is warmed up above  $T_c$  and all the trapped magnetic flux is expelled.

inversion symmetry and displays extremely small creep rates as well. However, for the latter compound, in a certain temperature interval, the weak initial logarithmic creep is followed after several thousand seconds by a much faster, avalanchelike, also logarithmic, decay. $24$ 

In general in superconductors with strong vortex pinning the critical current  $j_c$  is high. However, this is not the case in CePt<sub>3</sub>Si which has the lowest critical current  $[j_c(300 \text{ mK})]$  $= 1.8 \times 10^7$  A/m<sup>2</sup>] among the compared superconductors (Fig. [5](#page-3-13)). As the temperature is the relevant parameter in the thermally activated motion of vortices it is important to com-

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FIG. 4. (Color online) Comparison of the normalized relaxation rates  $S = \partial \ln(M) / \partial \ln(t)$  as function of temperature for different compounds in a log-log representation.

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FIG. 5. (Color online) Comparison of the normalized relaxation rates  $S = \partial \ln(M) / \partial \ln(t)$  and the critical current at  $T = 0.3$  K for different compounds. For each compound the left bar depicts *S* and the right one  $j_c$ .

pare the relaxation rates of the different compounds at the same temperature. The comparison depicted in Fig. [5](#page-3-13) has been done for *T*= 300 mK and in the framework of the Bean model which assumes a constant  $j_c(T) \propto H^*(T)/d$ , where *d* is the thickness of the platelike-shaped sample. In Fig. [5](#page-3-13) we also plot the critical currents at the same temperature as the relaxation rates in order to understand their relevance for the pinning process. If we compare the critical currents  $j_c$  of the two noncentrosymmetric compounds at *T*= 300 mK we find  $j_c$ (Li<sub>2</sub>Pt<sub>3</sub>B)/ $j_c$ (CePt<sub>3</sub>Si)  $\approx$  7. Even at the same  $T/T_c$  the critical current in CePt<sub>3</sub>Si is more than  $40\%$  lower in comparison with  $Li<sub>2</sub>Pt<sub>3</sub>B$ . Therefore, one conclusion deduced from Fig. [5](#page-3-13) is that the critical current is not the relevant parameter for the pinning mechanism in CePt<sub>3</sub>Si. A lower critical current for  $CePt<sub>3</sub>Si$  is reflected in a reduced vortex density which could explain the lack of avalanchelike relaxation.

The extremely slow vortex dynamics in  $CePt<sub>3</sub>Si$  in combination with the comparatively small critical current suggests that an unconventional and very effective pinning mechanism is at work. Similar effects had been seen in  $UPt<sub>3</sub>$ ,  $Sr<sub>2</sub>RuO<sub>4</sub>$ , and  $Pros<sub>4</sub>Sb<sub>12</sub>$  and have been associated with an intrinsic pinning mechanism on domain walls existing due to time-reversal symmetry violation in these superconductors.<sup>5</sup> However, CePt<sub>3</sub>Si does not break time-reversal symmetry. It has been recently proposed by Iniotakis *et al.*<sup>[21](#page-4-8)</sup> that twin boundaries in twinned crystals could play a similar role in noncentrosymmetric superconductors and yield a very strong flux-line pinning due to the fractionalization of vortices. So twin boundaries could act as planar barriers for flux flow without affecting the critical current. While this could be an explanation for the observed behavior in  $CePt<sub>3</sub>Si$  and also provides a possible mechanism for the flux avalanches reported for  $Li_2Pt_3B$ ,<sup>[24](#page-4-11)</sup> there has been no direct observation of such flux-line pinning on twin boundaries so far.

# **IV. CONCLUSION**

In conclusion, we observed extremely slow vortex dynamics in the noncentrosymmetric CePt<sub>3</sub>Si in spite of a very low critical current. The relaxation rates are comparable only to the similarly noncentrosymmetric  $Li<sub>2</sub>Pt<sub>3</sub>B$  which has as well a modest critical current though larger than in CePt<sub>3</sub>Si. This apparent contradiction of extremely low relaxation rates in conjunction with low critical currents indicates an unconventional and very effective flux trapping mechanism. A possible explanation of this pinning mechanism could be the existence of fractionalized vortices localized on the twin boundaries of the noncentrosymmetric crystal. However, this scenario needs independent verification apart from the flux dynamics reported here. No other explanations of the observed phenomena are known to us to date. Unlike in  $Li<sub>2</sub>Pt<sub>3</sub>B$  we did not observed flux avalanches.<sup>24</sup> This might be due to the much lower flux density reflected by the reduced critical current in  $CePt<sub>3</sub>Si$ .

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